

Optical analysis of the system

Simulation (TracePro 2.3)
of the YAP-QUARTZ system, source:
9200 photons at
390 nm for each gamma

- Q.E.: 20% ($\lambda_{\text{peak}}=390$ nm)
- Average optical collection factor (total reflection condition + bulk absorption L_a : 14 cm + reflection on the HPD window): 30%

Resulting average signal: 574 p.e. (sum of both sides)

Agreement with Prof. Seguinot's evaluation

ANGLE RECONSTRUCTION IN COMPTON INTERACTIONS

EGS4 simulation. Used approximations:

- Parallel incident rays
- Dead zone is vacuum (only YAP)
- No doppler broadening in Compton interactions
- Average 511 keV gamma pulse height: 574 p.e.

Method:

$$\text{P.H.} = 590 - 30 \times \min(z, L - z) \text{ p.e.}$$

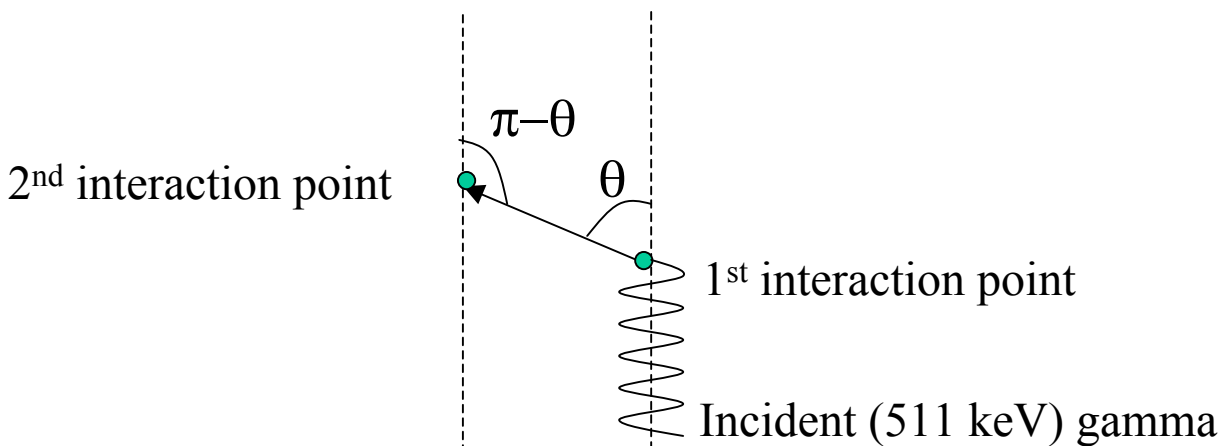
- θ_1 and θ_2 by energy deposit $E' = \frac{E}{1 + E(1 - \cos\vartheta) / m_e}$
 $\xrightarrow{E=511 \text{ keV}} \vartheta = \arccos(2 - E / (E - edep))$

- Comparison: if $\theta_1 - (\pi - \theta_2) > \Delta\theta_{\text{geom}}$ then the event can be reconstructed

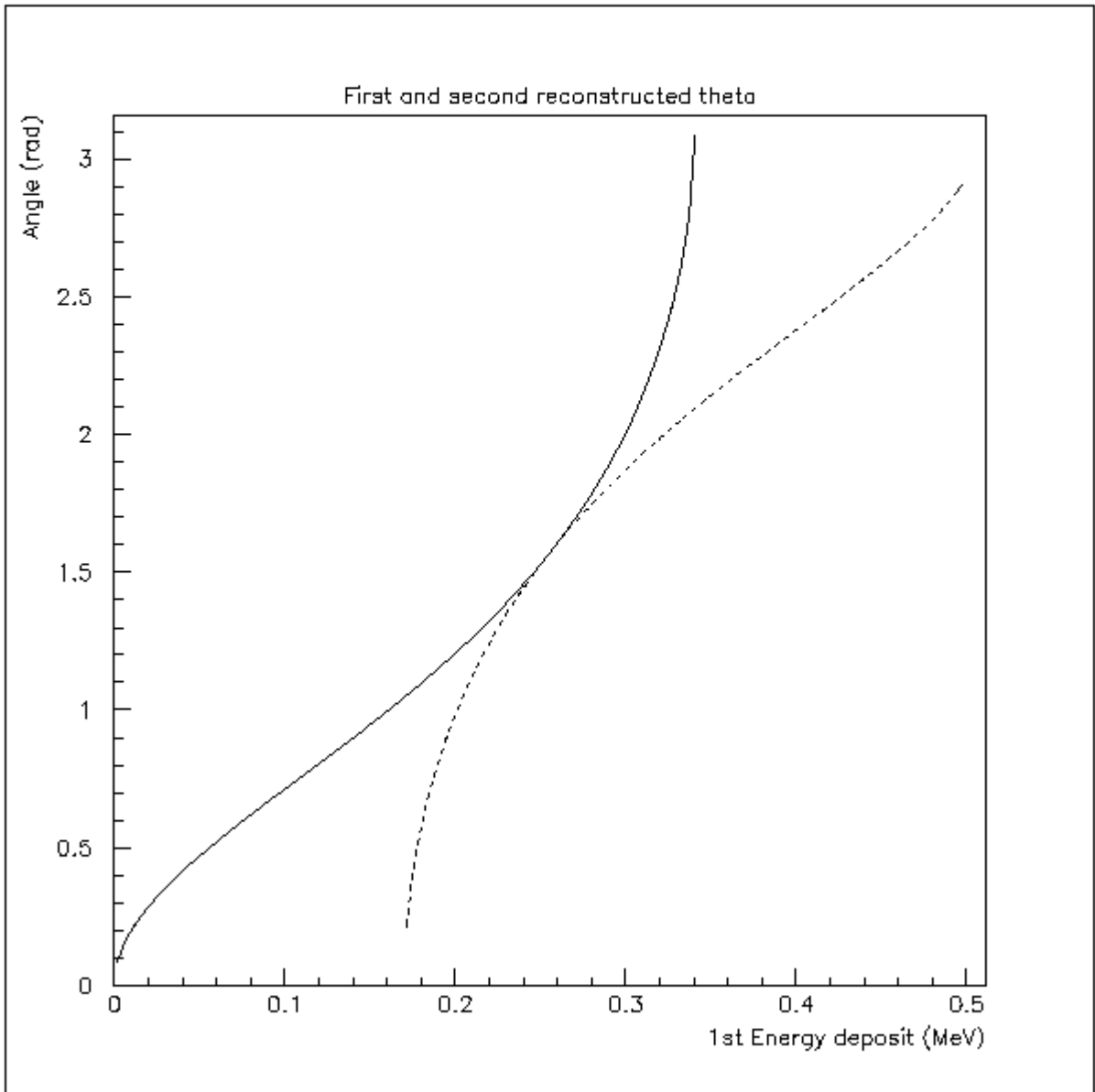
- Preliminary evaluation of $\Delta\theta_{\text{geom}}$ (not yet completely simulated the position reconstruction, two possible ways):

$$\Delta\vartheta = 2 \arcsin(|\Delta r^{\rho}| / dist) \rightarrow \text{Only } dist > 10 \text{ mm events}$$

$$|\Delta r^{\rho}| \leq \sqrt{2(\sqrt{2} \cdot 3.5 / 2)^2 + 5^2} \text{ mm} \sim 6.9 \text{ mm} \rightarrow \Delta\theta \sim 1.5 \text{ rad (bad)}$$



The scattering angle θ as function of the energy deposit (continuous line) and $\pi - \theta_{\text{rec}}$ by the second (photoelectric) energy deposit (dotted line). Ambiguity is expected in $\sim 200 - 300$ keV energy deposit range.



PET MODULE EGS SIMULATION

Simulated gammas: 10^5

Interacting gammas (N) : 83.7%

Totally absorbed

47.5% N

3.8% N: Ph (1 interaction)

8.7% N: C+ Ph

11.5% N: C+ C+ Ph (?)

23.5% N: more than 2 C + Ph (??)

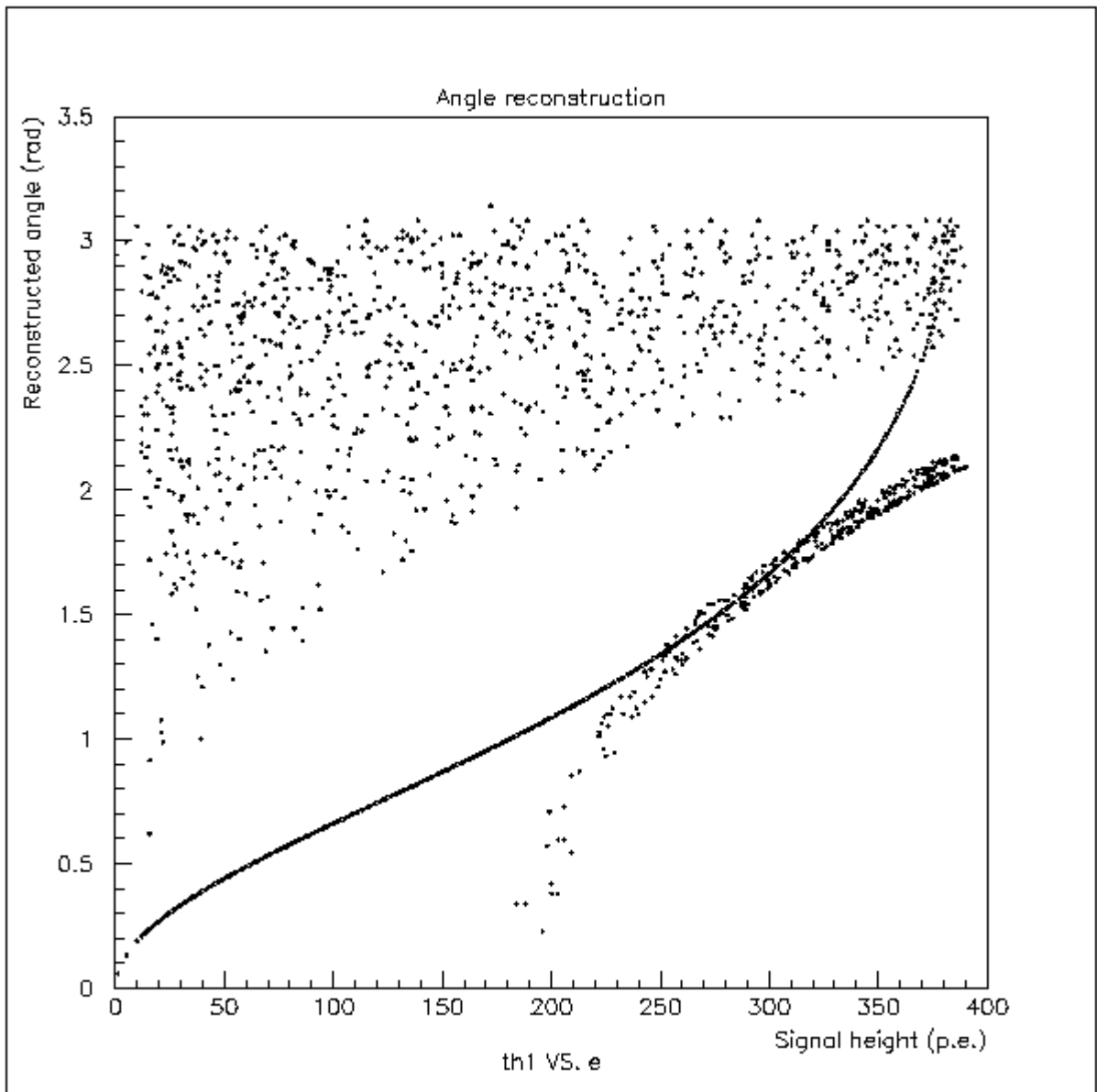
2.0% reconstructed

6.7% ambiguous

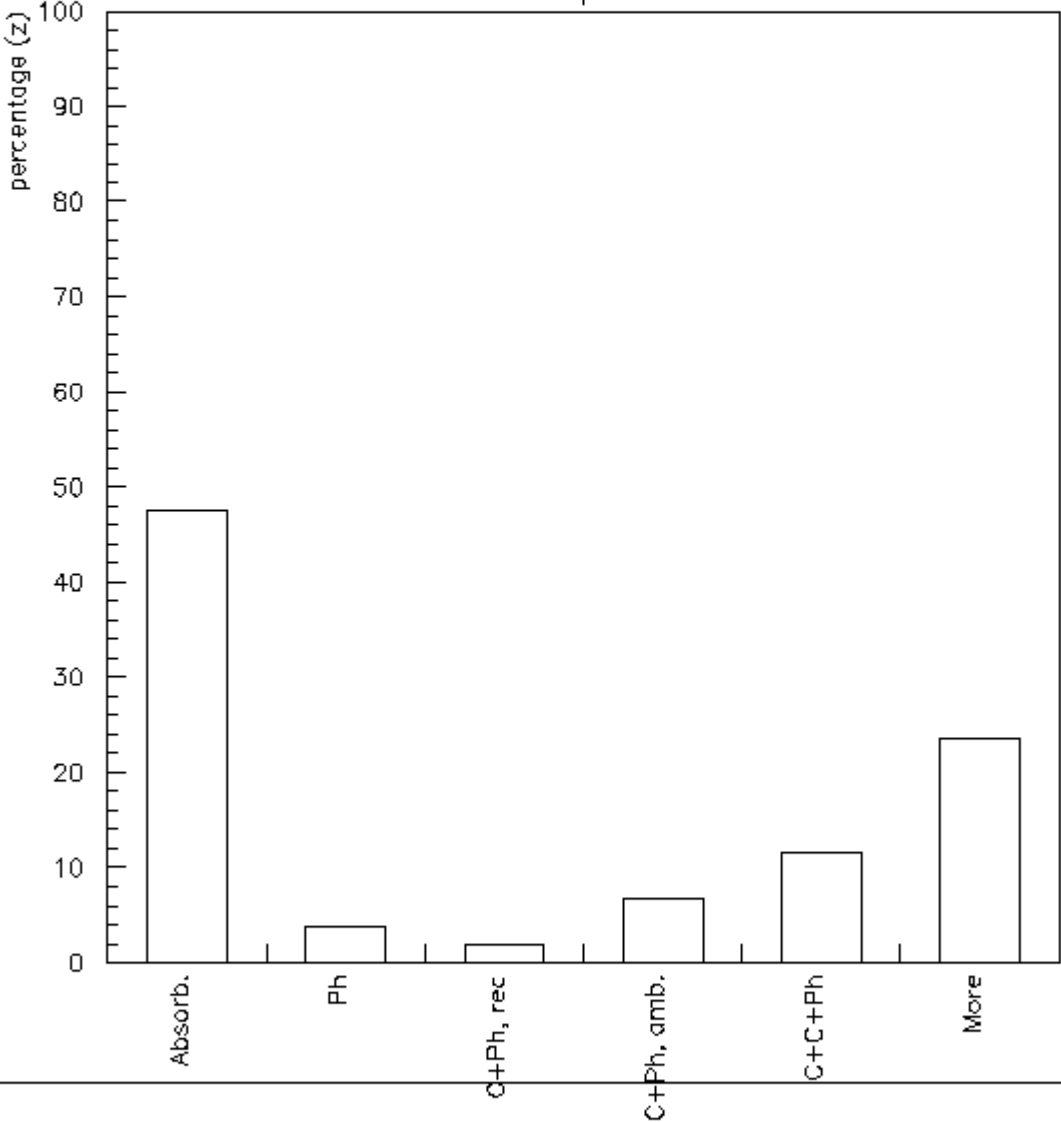
$$\text{Coincidence efficiency} = \epsilon_{\text{Ph}} \times \epsilon_{\text{Ph}} + \epsilon_{\text{rec}} \times \epsilon_{\text{rec}} + 2 \times \epsilon_{\text{rec}} \times \epsilon_{\text{Ph}} =$$
$$(0.038)^2 + (0.020)^2 + 2(0.035 \times 0.020) = 0.32\%$$

$$\text{Efficiency Gain} = 0.32\% / (3.8\%)^2 = 2.3$$

The Monte Carlo reconstructed scattering angle θ_1 as function of the pulse height and $\pi-\theta_2$ by the second energy deposit. High not-correlated values of $\pi-\theta_2$ are reconstructed in second Compton interaction case



PET module performance



TO BE DONE

- Angular reconstruction by points of interactions
- Analysis of the $C+C+Ph$ events
- Possibility of reconstruction of $C+C+C+Ph$ events?
- EGS simulation of the body (Compton from tissue)